

# Single and Multi-Objective Optimization Algorithms

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**Abstract**— Hybrid and multi optimization techniques are used extensively for solving optimal power flow problems. In this paper, particle swarm optimization (PSO), is incorporated with grey wolf optimization, (GWO) to form hybrid algorithm called HPSOGWO and using the multi-objective optimization of this algorithm, which called MO-HPSOGWO and comparing them. The HPSOGWO and MO-HP SOGWO are implemented to enhance the optimal power flow solution of IEEE-30 bus system. Five objective functions (OPF) optimizing separately by HPSOGWO and simultaneously in a single run by MO-HPSOGWO. The Matlab software is used to solve the system.

**Keywords**— Hybrid and multi optimization techniques, Multi optimization techniques, Single objective functions (OPF).

## I. INTRODUCTION

Optimization techniques are the best techniques for optimal results for any problem in any field. Traditional optimization techniques are less used due to its key disadvantage: local optimal solution [1, 2]. The modern optimization techniques are mostly used. It is adjusted by a set of random candidate solutions for a given problem in order to progress them over an adjusted number of steps. Optimization of real world problems requires handling various difficulties such as: multi-objectives [3], uncertainties [4], constraints [5], false global solutions [6], local solutions [7], despite of the advantages of these techniques.

A multi-objective optimization problem consists of a several objective functions more than one function [8]. There is a several non-dominated solutions for a multi-objective problem because of the problems nature [9]. On the other hand, a single objective problem is featured by only one global (best) solution.

There are two basic methods to solve multi-objective optimization problem: a posteriori versus a priori [3, 10]. For a priori method, we converted a multi-objective optimization problem to a single objective by a set of weights. In this method, an algorithm must be run multiple times to defined the Pareto optimal set, which is considered as the main disadvantages of this method. And some special Pareto optimal fronts cannot be defined with this method [11-13].

At A posterior method, multi-objective formulation of a multi-objective optimization problem is maintained to determine the Pareto optimal set by one run. Moreover, any type of Pareto front can be defined with this method. The main disadvantage of this method is that it has higher computational cost and managing multiple objectives at the same time. There are other popular optimization methods

such as: Multi-objective Grey Wolf Optimizer [14], Multi-objective Bee Algorithm [15], Multi-objective Particle Swarm Optimization [16, 17], Multi-objective Bat Algorithm [18], Non-dominated Sorting Genetic Algorithm [19-21].

Hybrid algorithms are a combination between two or more algorithms such as hybrid Particle Swarm Optimization with Gravitational Search Algorithm (PSOGSA) [22,23], and Particle Swarm Optimization with Dragonfly Algorithm (PSODA) [24], and Particle Swarm Optimization with Firefly Algorithm (PSOFA) [25], and Particle Swarm Optimization with Multi Verse Optimizer (PSOMVO) [26].

Regarding to the No-Free Lunch (NFL) theorem, there is no optimization technique for solving all optimization problems [27] making researchers are able to formulate new algorithms or improve it.

## II. PROBLEM FORMULATION

### A. Single objective OPF Problem Formulation

The mathematical formulation of the OPF problem is presented as a non-linearly constrained optimization problem:

$$u = [Q_C^T \quad TC^T \quad V_C^T \quad P_C^T]$$

Where:

$u$  = the control variables

$Q_C$  = reactive power supplied by all shunt reactors

$TC$  = magnitudes of transformer load tap changer

$V_G$  = voltage magnitude at generator buses

$P_G$  = active power generated at generator buses

$$x = [V_L^T \quad \theta^T \quad P_{SG} \quad Q_G^T]$$

Where:

$x$  = the state variables

$V_L^T$  = voltage magnitude at load buses

$\theta$  = voltage angles of all buses excluding the slack bus

$P_{SG}$  = active power generated at the slack bus

$Q_G$  = reactive power generated at all generator units

$N_L$  = load buses number

$N_G$  = generator buses number.

Optimization problem as OPF problem is presented as maximizing or minimizing objective function to be subjected to a set of equality and inequality constraints.

### B. Multi-Objective OPF problem Formulation

Multi-Objective optimization problem consists of several objective functions optimized simultaneously [28, 29]. The Multi-Objective OPF problem is presented as:

Minimize  $f(x)$  where

$$f(x) = [f_1(x)f_2(x)f_3(x)f_4(x)f_5(x)]$$

Subject to:

$$x \in X$$

Where  $X$  is a feasible region:

$$X = [x : x \in R^n, g_i(x) \leq 0, x_j \geq 0 \forall i, j]$$

where

$R$  = set of real numbers

$g_i(x)$  = set of constraints

$x$  = set of decision variables.

### III. PROBLEM OBJECTIVES

#### A. Fuel Cost Minimization

The economic distribution of a load defined among the different generators of a system, the variable operating costs must be presented as active power generated at each generator in a system. The fuel cost is the essential cost in a thermal or nuclear unit. Then the fuel cost must be presented as active power generated at each generator in a system. Other costs, such as the operation and maintenance costs, can also be presented as the power output. Fixed costs, such as the capital cost, depreciation ..., are not containing in the fuel cost.

A quadratic function of active power generated by each unit in a system approximates the fuel cost curve as:

$$F_1 = \sum_{i=1}^{N_G} (a_i + b_i P_{Gi} + c_i P_{Gi}^2) (Rs./h) \quad (1)$$

where:

$P_{Gi}$  is the active power generated at an  $i$ th generator in a system

$N_G$  is the generators number in a system

$a_i, b_i, c_i$  fuel cost coefficients of an  $i$ th generator in a system.

#### B. Emission Minimization

The function of emission can be aggregated of all types of emission considered, such as  $NO_x, SO_2$ , thermal emission, etc., As shown in this equation, the amount of emissions is presented as a function of active power generated at each generator in a system, which is the sum of quadratic and exponential functions:

$$F_2 = \sum_{i=1}^{N_G} [10^{-2} * (\alpha_i + \beta_i P_{Gi} + \gamma_i P_{Gi}^2) + \varepsilon_i \exp(\lambda_i P_{Gi})] (t/h) \quad (2)$$

where:

$\alpha_i, \beta_i, \gamma_i, \varepsilon_i$  and  $\lambda_i$  are the emission characteristics coefficients of the  $i$ th generator.

#### C. Total Real Power Loss Minimization

The term PL represents the total  $I^2R$  loss in the transmission lines and transformers of the system. From equation (3) total active power loss equal the sum of generated active power at each generator in a system subtract the sum of an active

power at each load bus in a system and the  $P_{loss}$  must be more than zero.

$$F_3 = P_L = \sum_{i=1}^N P_i = \sum_{i=1}^{N_G} P_{Gi} - \sum_{i=1}^{N_d} P_{di} \quad (3)$$

where

$P_i$  real power in each bus:

$P_{di}$  the demand real power

$N_d$  is the load buses number in a network.

$N_G$  is the generator buses number.

#### D. Reactive Power Transmission Loss Minimization

Reactive Power Transmission Loss Minimization lead to voltage stability margin (VSM) increasing and enhancing and guarantee good transportation real power from sources to sinks in a network and the  $Q_{loss}$  can be positive or negative value.

$$F_4 = Q_{loss} = \sum_{i=1}^N Q_i = \sum Q_{Gi} - \sum Q_{di} \quad (4)$$

#### E. Reactive Power Reserve Margin Maximization

Reactive Power Reserve Margin Maximization leads to minimize reactive power losses and to improve voltage stability and voltage stability under increased load condition or system disturbances. The fast reactive sources are generators, synchronous condensers and FACTS.

$$p_5 = \sum_{i=1}^{N_G} \left[ \frac{Q_i^2}{Q_{i\max}} \right] \quad (5)$$

### IV. PROBLEM CONSTRAINTS

#### A. Equality constraints

Equality constraints condition can be presented as:

$$\sum_{i=1}^{N_G} P_{Gi} - P_D - P_{loss} = 0 \quad (6)$$

Where  $P_D$  and  $P_{loss}$  are demand power and power losses, respectively.

$$\sum_{i=1}^{N_G} Q_{Gi} - Q_D - Q_{loss} = 0 \quad (7)$$

#### B. Inequality constraints

-Constraints of generation capacity

The generator outputs and bus voltage is restricted by min and max limits as:

$$P_{Gi}^{min} \leq P_{Gi} \leq P_{Gi}^{max} \quad (8)$$

$$Q_{Gi}^{min} \leq Q_{Gi} \leq Q_{Gi}^{max} \quad (9)$$

$$Q_i^{min} \leq Q_i \leq Q_i^{max} \quad (10)$$

$$v_i^{min} \leq v_i \leq v_i^{max} \quad (11)$$

- Constraints of line flow

This constraints can be presented as:

$$|P_{Lf,k}| \leq P_{Lf,k}^{max} \quad k = 1, 2, \dots, L \quad (12)$$

where,  $P_{L_f,k}$  is the active power flow of line k;  $P_{L_f,k}^{max}$  is the active power flow high limit of line k and  $L$  is the transmission lines number.

### V. THE PROPOSED ALGORITHMS

The mathematical model for each optimization techniques is explained in this section.

#### A. Particle Swarm Optimization (PSO)

The PSO algorithm was firstly invented by Kennedy and Eberhart in 1995 [30,31] and it is based on the imitation of the social behavior of fish, birds and insects and its movement with communication as bird flocking and fish schooling. The word particle indicates, for example, a bee in a colony or a bird in a swarm. Each individual or particle in a swarm be in a organized way by its own intelligence and the collective or group intelligence of the swarm. When one particle finds a good route to food, other particles in a swarm will also be able to follow the good path instantly even if their site is remote from the swarm. This optimization methods based on swarm intelligence are called behaviorally inspired techniques as opposed to the genetic algorithms, which are called evolution-based procedures. It is a population-based technique (a population of particles) and used for optimizing optimization problems. Each particle is supposed to have two characteristics (a position and a velocity). Each particle be around in the search space and can be the best position when evaluated the value of objective function. The particles can be updated a good positions and their velocities based on equations (14) and (15). This approach is learned from swarms behavior to optimize global optimization functions solution and every individual in the swarm is called a particle [32]. These mathematical equations are:

$$\omega = \omega_{max} - k * \frac{\omega_{max} - \omega_{min}}{Maxite} \quad (13)$$

$$V_{ij}^{k+1} = \omega * V_{ij}^k + c_1 * r_1 * (Pbest_{i,j}^k - X_{i,j}^k) + c_1 * r_1 * (Gbest_j^k - X_{i,j}^k) \quad (14)$$

$$X_{i,j}^{k+1} = X_{i,j}^k + V_{i,j}^{k+1} \quad (15)$$

Where, population size is indicated as N and dimension D is presented as  $X = [X_1, X_2, \dots, X_N]^T$ , where T indicates the transpose operator. Each particle is presented as  $X_i$  ( $i = 1, 2, \dots, N$ ) is presented as  $X_i = [X_{i,1}, X_{i,2}, \dots, X_{i,D}]$ . Also, the initial velocity of the population is indicated as  $V = [V_1, V_2, \dots, V_N]^T$ . Thus, the velocity of each particle in a population  $X_i$  ( $i = 1, 2, \dots, N$ ) is presented as  $V_i = [V_{i,1}, V_{i,2}, \dots, V_{i,D}]$ . The index  $i$  mutates from 1 to N whereas the index  $j$  mutates from 1 to D.

#### B. Grey Wolf Optimizer (GWO)

The GWO algorithm mimics the leadership hierarchy and hunting technique of grey wolves in nature submitted by Mirjalili et al. [33]. Grey wolves are considered to be at the top of food series and they are living in a collection. Four species of grey wolves such as alpha ( $\alpha$ ), beta ( $\beta$ ), delta ( $\delta$ ), and omega ( $\omega$ ) are simulating the leadership hierarchy and as basic parameters of GWO. As designing GWO according

to social hierarchy of wolves, considering the fittest solution as the alpha ( $\alpha$ ). The second and third best solutions are presented as beta ( $\beta$ ) and delta ( $\delta$ ), respectively. The residual of the candidate solutions are supposed to be omega ( $\omega$ ).

Three basic principles of GWO algorithm, namely hunting, chasing, and tracking for prey, encircling prey, and attacking prey which are considered as the behavior of grey wolves and using for designing GWO. The encircling behavior can be presented as:

$$\vec{D} = |\vec{c} \cdot \vec{X}_p(t) - \vec{X}(t)| \quad (16)$$

$$\vec{X}(t+1) = \vec{X}_p(t) - \vec{A} \cdot \vec{D} \quad (17)$$

where,  $t$  indicates the current iteration,  $D, A$ , and  $C$  indicate coefficient vectors,  $X_p$  is the prey position vector, and  $X$  denotes the grey wolf position vector. The vectors  $A$  and  $C$  are determined as :

$$\vec{A} = 2\vec{a} \cdot \vec{r}_1 - \vec{a} \quad (18)$$

$$\vec{C} = 2 \cdot \vec{r}_2 \quad (19)$$

simulating the hunting behavior of grey wolves, assuming that the alpha ( $\alpha$ ), beta ( $\beta$ ), and delta ( $\delta$ ) have better knowledge about the probable site of prey. The hunting behavior can be presented as :

$$\vec{D}_\alpha = |\vec{C}_1 \cdot \vec{X}_\alpha - \vec{X}|, \vec{D}_\beta = |\vec{C}_2 \cdot \vec{X}_\beta - \vec{X}|, \vec{D}_\delta = |\vec{C}_3 \cdot \vec{X}_\delta - \vec{X}| \quad (20)$$

$$\vec{X}_1 = \vec{X}_\alpha - \vec{A}_1 \cdot (\vec{D}_\alpha) \quad (21)$$

$$\vec{X}_2 = \vec{X}_\beta - \vec{A}_2 \cdot (\vec{D}_\beta) \quad (22)$$

$$\vec{X}_3 = \vec{X}_\delta - \vec{A}_3 \cdot (\vec{D}_\delta) \quad (23)$$

$$\vec{X}(t+1) = \frac{\vec{X}_1 + \vec{X}_2 + \vec{X}_3}{3} \quad (24)$$

At  $|A| < 1$ , the wolves are forced to attack the prey, where  $A$  is random value. Searching for prey is the exploration ability and attacking the prey is the exploitation ability. At  $|A| > 1$  the wolves are enforced to splay from the prey.

#### C. A Newly Hybrid Algorithm

There are a lot of hybridization techniques for heuristic techniques. According to Talbi [34,35], which can be hybridized two techniques or more for hybridization techniques. HPSOGWO is a combination of PSO and GWO. HPSOGWO combines the best strength of both PSO in exploration and in exploitation stage across the targeted optimum solution by replacing the best Value of PSO with grey wolf position value of GWO. In HPSOGWO, first three agents position is updated in the search space by the equations (25-27) with addition inertia constant ( $\beta$ ) to control the exploration and exploitation of the grey wolf in the search space. The modified equations are presented as:

$$\vec{D}_\alpha = |\vec{C}_1 \cdot \vec{X}_\alpha - \omega * \vec{X}| \quad (25)$$

$$\vec{D}_\beta = |\vec{C}_2 \cdot \vec{X}_\beta - \omega * \vec{X}| \quad (26)$$

$$\vec{D}_\delta = |\vec{C}_3 \cdot \vec{X}_\delta - \omega * \vec{X}| \quad (27)$$

Where,  $\omega$  denotes as inertia weight For combining PSO and GWO techniques, the velocity and updated equation are presented as:

$$V_{i,j}^{k+1} = \omega * V_{i,j}^k + c_1 * r_1 * (X_1 - X_{i,j}^k) + c_2 * r_2 * (X_2 - X_{i,j}^k) + c_3 * r_3 * (X_3 - X_{i,j}^k) \quad (28)$$

$$X_{i,j}^{k+1} = X_{i,j}^k + V_{i,j}^{k+1} \quad (29)$$

D. The basic steps of HPSOGWO

- STEP 1:** Create an initial population (agents) or (Grey wolves).
- STEP 2:** Initialize a,A,C and  $\omega$  equations( 13,18,19).
- STEP 3:** Fitness evaluation of each agents.
- STEP 4:** Calculate the position of Grey Wolf. $X_\alpha, X_\beta, X_\delta$  equations(25-27) and (21-23).
- STEP 5:** Updating velocity and position equations(28,29).
- STEP 6:** Repeat STEP (2-5) until the stop criteria is reached.
- STEP 7:** Stop.

VI. MULTI-OBJECTIVE OPTIMIZATION

Multi-Objective optimization problem consists of several objective functions to be optimized simultaneously. In these problems, objective functions are in conflicting with each other. For example, in Optimal Power Flow problem (OPF), by minimizing generation fuel cost and consequently active and reactive power losses are maximizing. Main concepts related to Multi-Objective Optimization are [36]:

A. Domination

In Multi-Objective optimization the domination is used for comparing the solutions as in Fig 1. If all the X1 solution are not worse than all solution X2 in all objectives, or if all the X1 solutions are equal to X2 but only in one case or one dimension X1 is better than X2, then it can be said that X1 will dominate X2 and X2 must be deleted from solutions list. The mathematical expression of the domination part is presented as :

$$x_1 \text{ dominate } x_2 \text{ if:} \\ f(x_1) \leq f(x_2) \\ f(x_1) < f(x_2)$$

B. Pareto front

A solution of Multi-Objective optimization problem is a curve not a point but a set of points, which every point in this curve will non-dominate each other. Because if find a point in which one of the target functions is minimum, there is another target function which is not minimum at this point. This curve called Pareto front curve as in Fig 2.

C. Finding best local guide

A solution of Multi Objective optimization problem is a set of Pareto optimal solutions not the best point. Pareto

optimal solutions obtained in each iteration are stored in an archive (Repository) and this archive is updated in each iteration to make the domination points deleted. All the Pareto optimal solutions in the archive are equally good.

VII. D. A MULTI-OBJECTIVE HYBRID ALGORITHM (MO-HPSOGWO)

In order to implement multi-objective optimization by HPSOGWO we combine two new components. The components are similar to MOPSO [17,18] and MOGWO [21].The first one is the repository (archive), which is responsible for storing non-dominated Pareto optimal solutions obtained so far and there is a maximum number of solutions for the repository. The second component is a leader selection designing that assists to select alpha, beta and delta solutions as the leader of the hunting process from the repository.

The MO-HPSOGWO algorithm inherits all the characteristics of HPSOGWO, which means that there are the same exploration and exploitation abilities in two algorithms. The basic difference that MO-HPSOGWO design about the repository (archive), which the solution is a set of non-dominated solutions not three best solutions as HPSOGWO algorithm.

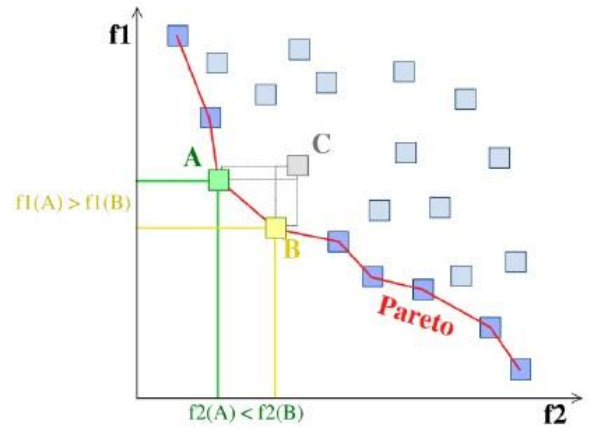


Fig.1. Pareto optimum [37]

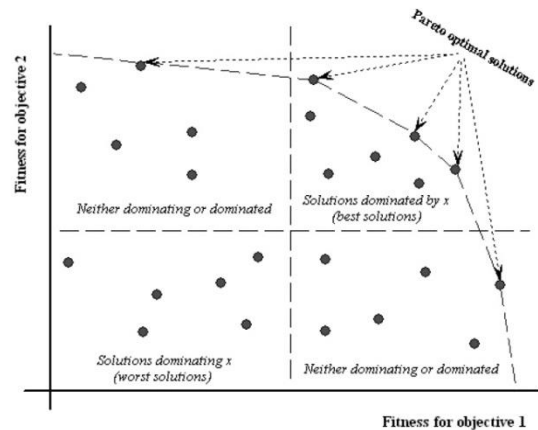


Fig.2. Concept of pareto optimality [38]

VIII. PSEUDO CODE OF THE MO-HPSOGWO ALGORITHM

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Create an initial population  $X_i(i = 1, 2, \dots, n)$ 
Initialize a, A, C and  $\omega$  equations(13,18,19)
Fitness evaluation of each agents
Find the non-dominated points and initialized the
repository with them
 $X_\alpha = \text{SelectLeader(rep)}$ 
Exclude  $\alpha$  from the repository tentatively to avoid selecting
the same leader
 $X_\beta = \text{SelectLeader(rep)}$ 
Exclude  $\beta$  from the repository tentatively to avoid selecting
the same leader
 $X_\delta = \text{SelectLeader(rep)}$ 
Add back alpha and beta to the repository
t=1;
for (t=1: Max iterations)
for each agents
Update the position of the current search agent by
equations(25-27) and (21-23)
Update the velocity and position by equations (28,29) end
for
Update a, A, C and  $\omega$ 
Fitness evaluation of each agents
Find the non-dominated points
Update the repository
If the repository is complete
Run the grid mechanism to delete one of the current
repository points
Add the new point to the repository
end if
 $X_\alpha = \text{SelectLeader(rep)}$ 
Exclude  $\alpha$  from the repository tentatively to avoid selecting
the same leader
 $X_\beta = \text{SelectLeader(rep)}$ 
Exclude  $\beta$  from the repository tentatively to avoid selecting
the same leader
 $X_\delta = \text{SelectLeader(rep)}$ 
Add back alpha and beta to the repository
t = t+1;
return rep
    
```

IX. RESULTS AND DISCUSSION

shown in Fig.9 The total active power demands is 283.4 MW and Total reactive power demands is 126.2 MVAR. Five objective functions (OPF) are individually optimized as a single objective function in optimization process by using HPSOGWO and are optimized simultaneously by using MO-HPSOGWO, which are :

- $F_1$  Fuel Cost Minimization
- $F_2$  Emission Minimization
- $F_3$  Total Active Power Loss Minimization
- $F_4$  Reactive Power Transmission Loss Minimization
- $F_5$  Reactive Power Reserve Margin Maximization.

From TABLE III : in single optimization process there is one best (global) solution for each function without attention to the value of the other four functions. For example, when minimizing of generation fuel cost this leads to active and reactive power losses in a system increasing and vice versa.

From TABLE IV : there are several solutions (non-dominated) for five functions (OPF) as in Fig.8, which are optimized simultaneously. And these five functions are conflicting objectives that means when decision optimal solution need to trade off between them. So the decision maker (DM) for selecting a compromise solution based on maximum limits as in TABLE II and minimum limits as in TABLE III.

TABLE I. Load flow analysis of 30 bus system by using NR method

Bus No.	V(p.u.)	Delta	P(MW)	Q(MVAR)
1	1.050	0.0	353.099	-14.98
2	1.038	-3.705	54.28	18.011
3	1.011	-10.514	-145.380	10.748
4	1.019	-8.316	-15.700	12.855
5	1.091	-8.667	24.280	22.753
6	1.091	-10.383	24.000	20.940
7	1.006	-9.554	-45.600	-10.900
8	1.016	-6.857	-15.200	-1.600
9	1.048	-9.932	0.000	0.000
10	1.031	-11.672	-11.600	-2.000
11	1.023	-5.708	-4.800	-1.200
12	1.065	-11.212	-22.400	-7.500
13	1.015	-7.994	0.000	-0.000
14	1.047	-12.088	-12.400	-1.600
15	1.039	-12.108	-16.400	-2.500
16	1.043	-11.666	-7.000	-1.800
17	1.030	-11.876	-18.000	-5.800
18	1.024	-12.654	-6.400	-0.900
19	1.019	-12.787	-19.000	-3.400
20	1.021	-12.565	-4.400	-0.700
21	1.019	-12.132	-35.000	-11.200
22	1.020	-12.119	-0.000	0.000
23	1.023	-12.434	-6.400	-1.600
24	1.009	-12.527	-17.400	-6.700
25	1.010	-12.469	-0.000	-0.000
26	0.993	-12.894	-7.000	-2.300
27	1.020	-12.163	0.000	0.000
28	1.012	-8.478	0.000	0.000
29	1.000	-13.401	-4.800	-0.900
30	0.989	-14.290	-21.200	-1.900

TABLE II. IEEE 30-bus system individual objective functions before applying optimization technique

Objective function	Objective value
Over all Generation fuel costs	4205.1 (\$/h)
Emission index	2.4681 (t/h)
Active power transmission loss	19.579 (MW)
Reactive power transmission loss	5.827 (MVar)
Reactive power reserve margin	1.1034

TABLE III. Single objective function values by HPSOGWO.

Function	Best solution
F <sub>1</sub> (min of fuel cost)	739.838
F <sub>2</sub> (min of emission)	2.0486E-04
F <sub>3</sub> (min of active power loss)	5.28
F <sub>4</sub> (min of reactive power loss)	-16.02
F <sub>5</sub> (max of reactive power reserve)	1.17E-16

TABLE IV. Multi-objective functions (OPF) values (non-dominated solutions) by MO-HPSOGWO

NO.	G <sub>FC</sub> (Rs/h)	E <sub>I</sub> (t/h)	P <sub>loss</sub> (MW)	Q <sub>loss</sub> (MVar)	R <sub>PRM</sub> (p.u)
1	778.892	0.0904	0.901	3.501	0.806
2	1628.2	1.1583	11.581	-7.867	0.213
3	805.713	0.1356	1.354	2.016	0.931
4	785.456	0.0487	0.484	10.316	1.086
5	976.827	0.3706	3.704	-0.181	0.711
6	787.768	0.0011	0.008	8.575	1.377
7	779.825	0.0134	0.132	10.625	1.053
8	1067.4	0.4988	4.986	-2.586	0.223
9	823.879	2.48E-04	2.36E-04	14.316	1.376
10	799.699	0.013	0.129	12.327	1.156
11	805.841	0.132	1.317	4.186	0.584
12	1054.9	0.4445	4.442	-0.419	0.663
13	858.655	0.1986	1.983	3.199	0.695
14	803.943	2.91E-04	4.59E-04	12.252	1.249
15	772.455	0.0506	0.504	5.517	1.143
16	938.129	0.3297	3.295	0.830	0.630
17	986.147	0.3724	3.722	0.239	0.483
18	812.773	0.0038	0.035	10.605	1.248
19	1885.6	1.449	14.494	-10.689	0.142
20	806.641	3.05E-04	4.44E-04	11.896	1.573
21	794.102	0.0168	0.165	10.329	0.990
22	1360.5	0.8531	8.528	-6.064	0.312
23	888.950	0.2575	2.573	0.417	0.720
24	1332.4	0.8148	8.145	-5.114	0.423
25	765.056	0.0227	0.224	5.935	1.398
26	854.473	0.1956	1.954	3.593	0.668
27	858.135	0.2078	2.076	2.245	0.558
28	761.863	0.0634	0.632	5.078	0.857
29	783.092	0.0165	0.163	10.118	1.122
30	819.717	4.15E-04	0.002	11.945	1.461
31	786.184	0.0061	0.059	9.857	1.398
32	781.588	0.0067	0.064	8.211	1.675
33	804.136	0.0856	0.854	7.028	0.846
34	1477.9	0.9816	9.814	-6.846	0.309
35	1992.6	1.5829	15.826	-12.984	0.258
36	772.595	0.0493	0.491	6.269	1.109
37	1008.3	0.4093	4.090	0.227	0.703
38	774.865	0.0343	0.340	6.896	1.326
39	778.702	0.0255	0.253	9.663	1.128
40	773.374	0.0544	0.542	6.308	0.843

TABLE V. The standard values used

Parameters	quantity
population size	100
Repository size (rep)	100
No. of iterations	200

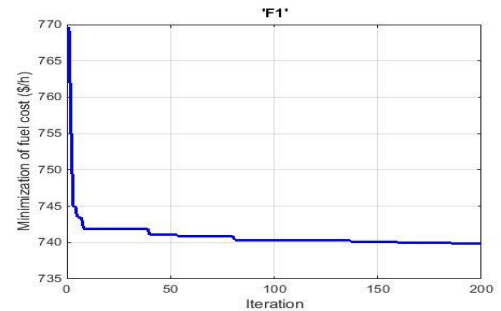


Fig.3. Minimization of generation fuel cost by HPSOGWO

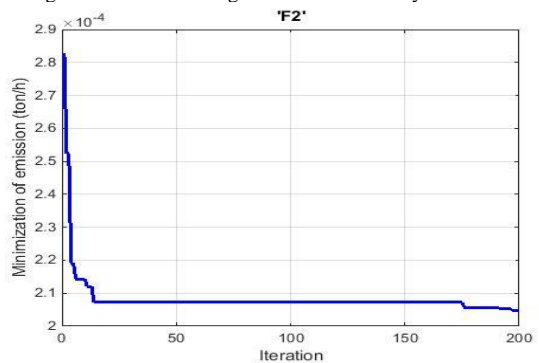


Fig.4. Minimization of emission by HPSOGWO

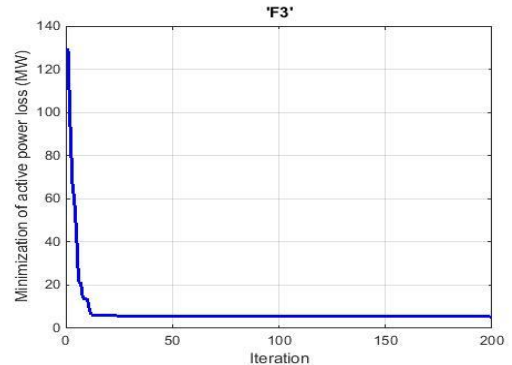


Fig.5. Minimization of active power loss by HPSOGWO

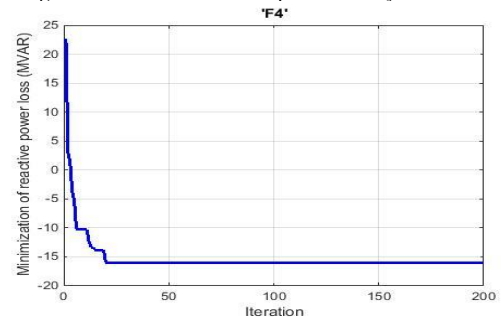


Fig.6. minimization of reactive power loss by HPSOGWO

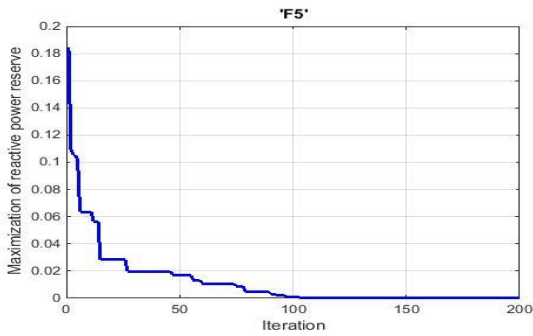


Fig.7. maximization of reactive power reserve margin by HPSOGWO

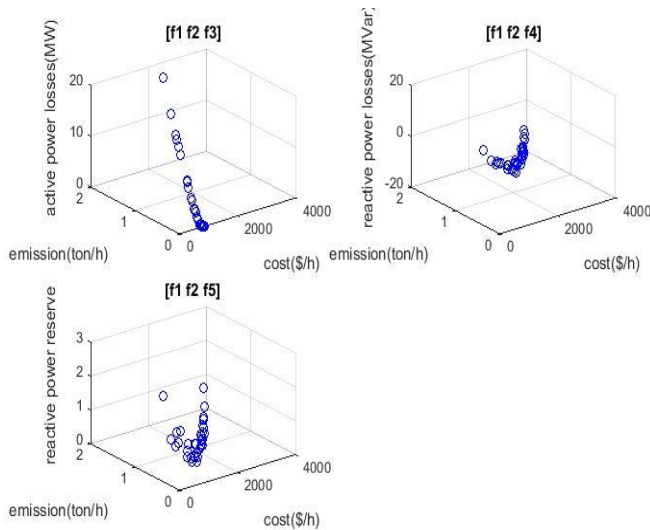


Fig.8. Pareto optimal for five function (OPF) non-dominated solutions by HPSOGWO

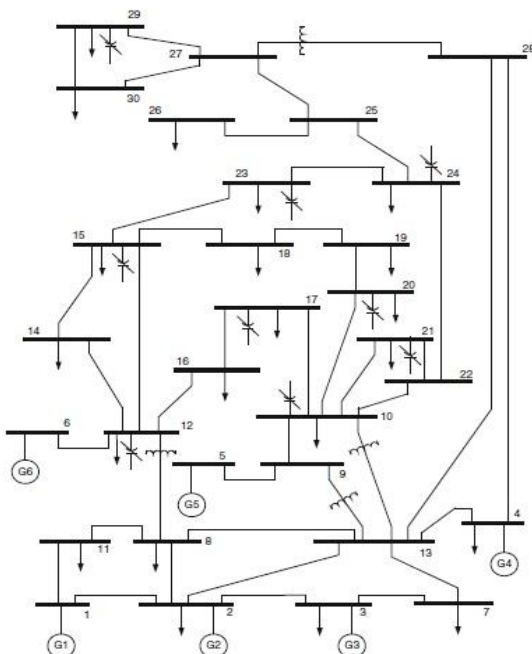


Fig.9. Single-line diagram of IEEE-30 bus test system

X. CONCLUSION

Most of the real world problems in many fields science, engineering, economics and logistics are multi-objectives optimization problems, making conflicting objectives. In this paper using two algorithms HPSOGWO and MO-HPSOGWO testing through IEEE 30-bus system and optimizing five objective function (OPF). From results MO-HPSOGWO is more realistic and efficient than HPSOGWO because single objective function (HPSOGWO) has one global solution without attention to the value of the other four functions as in TABLE III but multi-objective solutions (MO-HPSOGWO) has a set of non-dominated solutions and the compromise solution selecting based on decision maker (DM) as in TABLE IV and these five functions can be optimized concurrently. So without using multi-objective optimization in (OPF) only one aspect of the power system has been optimized.

XI. REFERENCES

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